

# Online Motion Planning MA-INF 1314

## Example questions

Elmar Langetepe

Universität Bonn, Institut für Informatik

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- ① CFS Algorithm  
Example in detail
- ② STC-Algorithms  
Scan-Variant
- ③ Online Navigation  
Lower bound construction

# General: For any configuration

- ① Precise model
- ② Strategy/Algorithm
- ③ Correctness
- ④ Lower Bound
- ⑤ Upper Bound
- ⑥ Structural properties, proofs
- ⑦ Main statements
- ⑧ Extensions, Applications, Remarks

# General: Lemmata/Theorems

- ① Top/Down
- ② Main statements
- ③ How did we achieve them?
- ④ Lemmata
- ⑤ Structural properties

- 1 Definition: Grid-environment, online, vertices, simple, neighboring cells
- 2 Theorem: Number of steps  $C + 1/2 E - 3$
- 3 Strategy Idea: SmartDFS, split-cell, recursion, quadrant  $Q$  by layer,
- 4 L-Offset-Lemma: 8/ edges less!
- 5 Shortest-Path-Lemma:  $1/2E - 2$
- 6 Edge-Lemma for  $Q$ :  $E(P_1) + E(P_2) = E(P) + E(Q)$
- 7 Excess-Lemma:  $excess(P) \leq excess(P_1) + excess(K_2 \cup \{c\})$
- 8 Proof Theorem: Induction! Apply Lemmata!

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# CFS Algorithm

- 1 Precise model: Constrained graph exploration, edges and vertices, Tether variant vs. Accumulator variant, depth restriction variant
- 2 Strategy/Algorithm: CFS, example application
- 3 Correctness: By construction
- 4 Lower Bound:  $E + V$
- 5 Upper Bound:  $(4 + 8/\alpha)E$  (more precisely:  $\Theta(E + V/\alpha)$ )
- 6 Structural properties and poofs: Proof of the invariants, analysis of the cost
- 7 Main statements: Competitive online exploration, UB, depth restricted, lookahead
- 8 Extensions, Applications, Remarks: Search ratio approximation, adjustments for unknown depth, simulate accu-variant by tether-variant, lookahead is necessary (accu)

# STC Algorithms

- 1 Precise model: Exploration, 2D cell, visit all cells by the tool, scan the 4 neighbourhood of 2D cells. Return variant!
- 2 Strategy/Algorithm: Spanning Tree construction online (DFS), Tool left hand side
- 3 Correctness: Visit all 2D cells that can be entered
- 4 Lower Bound: Visit all cells C (Hamiltonian path!)
- 5 Upper Bound:  $C + K$  (Boundary cells)
- 6 Structural properties, proofs: Example execution and analysis! Inner/Intra double visits
- 7 Main statements:  $C + K$ , 2-competitive, optimal in pure 2D scenes, Tightness for corridors
- 8 Extensions, Applications, Remarks: Scan-STC, **avoid spanning tree edges of a special kind, simple heuristic/analysis:  $H_{opt} + \text{Column-Divergence} + 1$**



# Online Navigation

- 1 Precise model: Touch sensor, coordinates of the goal, two different movements
- 2 Strategy/Algorithm: BUG variants, example executions, intention
- 3 Correctness: Closer to the goal, leave condition, enclosed?
- 4 Lower Bound: Distance to the goal, plus circumference of the the obstacles
- 5 Upper Bound: Depending on the variant
- 6 Structural properties and proofs: BUG2, intersections, tight bounds, estimating the movement in the free space, LB construction circumference
- 7 Main statements: Correctness, robust strategies, performance
- 8 Extensions, Applications, Remarks: Change1, Change2, Visibility