

Online Motion Planning, SS 16  
Exercise sheet 5  
University of Bonn, Inst. for Computer Science, Dpt. I

- *You can hand in your written solutions until Wednesday, 25.5., 14:15, postbox in front of room E.01 LBH.*
- *We allow (and recommend) fixed groups of 2 students.*
- *Please subscribe to our mailing list:  
<https://lists.iai.uni-bonn.de/mailman/listinfo.cgi/vl-online>*

**Exercise 13: Proof detail ccw-order turn (4 points)**

In the lecture there was a proof that shows that a curve from  $\mathcal{K}$  cannot have a self-intersection. We considered the case of a clockwise turn. Now consider the case of the counterclockwise turn (as in Figure 1) and analogously give the proof.

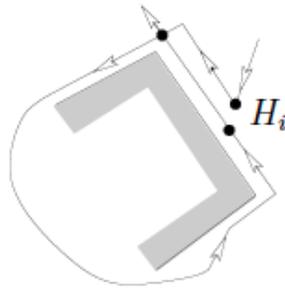


Figure 1: A counterclockwise loop and an intersection!

**Exercise 14: Detect vertical edges (4 points)**

We introduced  $\delta$ -pseudo orthogonal scenes with sensor error  $\rho$  and provide some sufficient condition in a **Corollary** for detecting a horizontal edge.

- a) By the same arguments and conditions, show that we can also correctly detect a vertical edge.
- b) Analogously, for moving along the boundary give sufficient conditions for detecting the case that two adjacent edges are *both* vertical edges (in principle).

**Exercise 15: Bug leaving from closest vertex (4 points)**

We consider a modification to the *BUG* algorithm, given that the obstacles are simple polygons in the plane. The bug starts at its starting point  $s$ . In order to reach destination point  $t$ , the bug moves in direction of  $t$ , until an obstacle  $O$  hinders its movements. As usual, the bug walks along the boundary of  $O$  and keeps track of the distance to  $t$ .

The modification is as follows. Instead of leaving  $O$  at a point closest to  $t$ , the bug leaves  $O$  at a *vertex*  $v$  of  $O$ 's boundary which is closest to  $t$ . Then, the bug continues in direction of  $t$ , until it encounters another obstacle.

Prove or disprove that the modified *BUG* algorithm will eventually reach the target point  $t$ , although possibly not as quickly as the unmodified algorithm.

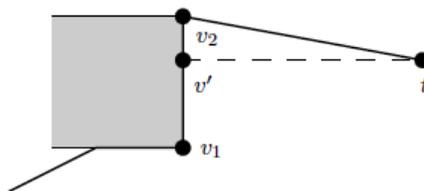


Figure 2: Bug-Variant: Leaving from the closest vertex  $v_2$ !